# Optimal Flocking Control for a Mobile Sensor Network Based a Moving Target Tracking

Hung Manh La School of Electrical and Computer Engineering Oklahoma State University Stillwater, OK, 74078, USA hung.la@okstate.edu Trung Hien Nguyen\* (nguyenhientrung@tnut.edu.vn),
Cong Huu Nguyen\*\* Hien Nhu Nguyen\*
Electrical Engineering Department\*
Electronics Engineering Department\*\*
Thai Nguyen University of Technology, Thai Nguyen, Vietnam

Abstract—Target tracking is an important task in sensor networks, especially in mobile sensor networks. Flocking control is used to control a mobile sensor network to track a target. However, there are some existing problems in this control method, such as the problem of how to design an optimal flocking control algorithm with optimal flocking parameters to allow the network to catch up the target as fast as possible in order to minimize the tracking time and power consumption. This paper presents an optimization problem in flocking control for a mobile sensor network to track a moving target. A non convex optimization method based on genetic algorithms is developed. The overall purpose of this approach is to find out the optimal solutions of flocking parameters that deliver desired swarm behaviors to minimize the cost function. This cost function represents the time it takes all mobile sensors (robots) in the network to catch up the moving target. The experimental tests are obtained to demonstrate our approach.

Keywords: Flocking control, Target tracking, Mobile sensor networks, Evolutionary algorithms.

# I. INTRODUCTION

# A. Motivation

Sensor networks [1], especially mobile sensor networks [2] have been extensively studied in recent years. Mobile sensor networks have several advantages over stationary sensor networks such as the adaptation to environmental changes and recon@urability for better sensing performance. Therefore mobile sensor networks can be applied in many applications such as target tracking [3] in underwater submarine detection and protection of endangered species [4]. Here we consider a mobile sensor in a mobile sensor network as a mobile robot which is equipped motors or actuators made by arti@ial muscle such as Ionic Polymer Metal Composite (IPMC) [5] for mobility, and camera, sonar or laser for target sensing and navigation.

A main issue for multiple mobile sensors to track a moving target is that these sensors have to move together without collision among them during tracking which requires the use of cooperative control methods [6], [7], [8], [9]. One of these methods is cocking control [10]. We know that cocking is a phenomenon in which a number of mobile agents move together and interact with each other while ensuring no collision, velocity matching, and cock centering [11]. In nature, schools of Csh, birds, ants, and bees, etc. demonstrate the phenomena of cocking. The problem of cocking has been studied for many

years. It has greatly attracted many researchers in physics [12], [13], mathematics [14], biology [15], and especially in control science in recent years [10], [16], [17], [18], [19], [20], [21], [22], [23], [24], [25].

The optimization problem of dynamic target tracking in a mobile sensor network is that how fast each member in the network can catch up the target while maintaining the network formation. An important issue of the ability to perform fast computational of cocking dynamics is to optimize the interaction of the cock members so that they can obtain the desired task. In order to achieve such purpose, this paper develops a genetic algorithm to tackle the objective function which is non convex and non-differentiable where the classical gradient-based optimization techniques are not robust and usually trapped by the local minima.

## B. Related Work

In this section, we review existing works in cocking control which are related to our approach.

Flocking control has been studied by many researchers. Wang and Gu [19] presented a survey of recent research achievements of robot cocking. Their paper gave an overview of the related basic knowledge of graph theory, potential function, network communication and system stability analysis. In [10], a theoretical framework for design and analysis of distributed cocking algorithms was proposed. These algorithms solved the cocking control in the absence and presence of obstacles. The static and dynamic virtual leaders were used as a navigational feedback for all mobile agents. An extension of the cocking control algorithms in [10], cocking of agents with a virtual leader in the case of a minority of informed agents and in the case of varying velocity of virtual leader, was presented in [16] and [17]. La and Sheng [26], [27], [28], [29] proposed the distributed cocking control with Single-CoM (Center of Mass) and Multi-CoM to improve the tracking performance in the obstacle space, and to deal with the complex or changing environment they proposed the distributed adaptive cocking control algorithm that can allow the network maintains the connectivity, tracking performance and similar formation in both free and obstacle spaces. In addition, to solve the problem of slitting/merging mobile agents in the case of multiple dynamic targets tracking they proposed the Seed Growing

Graph Partition (SGGP) algorithm. The SGGP algorithm allows the network to automatically decompose into multiple sub-groups to track multiple targets in term of minimizing the power consumption and time consuming. Shi and Wang [18] investigated the dynamic properties of mobile agents for the case where the state of the virtual leader is time varying and the topology of the neighboring relations between agents is dynamic was proposed. Anderson et al. [20] demonstrated a new technique for generating the constrained group animations of œocks in which users can impose constraints on agents positions at any time in the animation, or control the entire group meeting the shape constraints. Tanner et al. [21], [22] studied the stability properties of a system of multiple mobile agents with double integrator dynamics in the case of Exed and dynamic topology. In addition, the experimental implementation of cocking algorithms proposed in [21] and [22] on wheeled mobile robots was presented in [23]. Gervasi and Prencipe [24] studied the distributed coordination and control of a set of asynchronous, anonymous, memoryless mobile vehicles in the case of no communication among the vehicles. In particular, their paper analyzed the problem of cocking in a certain pattern and following a designated leader vehicle, while maintaining the pattern. Olfati-Saber [30] addressed a distributed cocking algorithm for mobile sensor networks to track a moving target. In his paper, an extension of a distributed Kalman Etering algorithm was used the sensors to estimate the target s position. In [25], a scalable multi-vehicle platform was developed to demonstrate a cooperative control algorithm in mobile sensor networks. Their cocking algorithm was implemented with Give TXT-1 monster truck robots.

In summary, in the cocking control most of existing works focused on the coordination, formation and splitting/merging problems in both Oked and switching topologies. In addition, the problem of controlling the size of the network in adaptive and decentralize fashion to deal with complex environment and the problem of designing the cocking control to deal with multi-target have been studied. However, the problem of how to design an optimal cocking control algorithm with optimal cocking parameters to allow the network to catch up the target as fast as possible to minimize the tracking time and power consumption is still an open research.

The rest of this paper is organized as follows. In the next section we present the distributed  $\infty$ cking control algorithm with obstacle avoidance for a moving target tracking and problem formulation. Section III presents the optimization problem of  $\infty$ cking control via genetic algorithms. Section IV presents the experimental tests. Finally, the conclusion of this paper is given in the Section V.

# II. FLOCKING CONTROL AND PROBLEM FORMULATION

# A. Distributed cocking control algorithm

We consider n robots moving in an m dimensional Euclidean space. We address the motion control problem for a robot group with the objective of dynamic target tracking. In this problem we suppose that each robot has a limited

communication range to allow it to communicate with others and to sense the target.

The dynamic equation of each robot is described as follows:

$$\begin{cases}
\ddot{E} = p_i \\
\dot{E} = u_i, \quad i = 1, 2, \dots, n
\end{cases}$$
(1)

here  $q_i, p_i \in \mathbb{R}^m$  (e.g.,m = 2, 3) are the position and velocity of robot i, respectively.

Given an communication range r, each mobile robot only interacts with a set of its neighborhood at time t as follows:

$$N_i(t) = \left\{ j \in \vartheta : ||q_j - q_i|| \le r, \ \vartheta = \{1, 2, ..., n\}, i \ne j \right\}$$
 (2)

where  $\|.\|$  is the Euclidean norm.

The dynamic topology of all mobile robots is considered as a dynamic graph  $G(\vartheta,E)$  consisting of a vertex set  $\vartheta = \{1,2...,n\}$  and an edge set  $E \subseteq \{(i,j): i,j \in \vartheta, j \neq i\}$ . In this topology each vertex denotes one member of  $\operatorname{cocks}$ , and each edge denotes the communication link between two members.

The geometry of cocks is modeled by  $\alpha$ -lattices [10] that has the following condition:

$$||q_i - q_j|| = d \tag{3}$$

here d is a positive constant indicating the distance between robot i and its neighbor j.

Firstly, based on Olfati-Saber s cocking algorithm with obstacle avoidance [10] we design a cocking control algorithm with a dynamic  $\gamma$ -agent. In this scenario, the dynamic  $\gamma$ -agent is considered as a moving target.

$$u_{i} = c_{1}^{\alpha} \sum_{j \in N_{i}^{\alpha}} \phi_{\alpha}(\|q_{j} - q_{i}\|_{\sigma}) n_{ij} + c_{2}^{\alpha} \sum_{j \in N_{i}^{\alpha}} a_{ij}(q) (p_{j} - p_{i})$$

$$+ c_{1}^{\beta} \sum_{k \in N_{i}^{\beta}} \phi_{\beta}(\|\mathcal{G}_{\ell,k} - q_{i}\|_{\sigma}) \mathcal{H}_{\ell,k} + c_{2}^{\beta} \sum_{k \in N_{i}^{\beta}} b_{i,k}(q) (\mathcal{F}_{\ell,k} - p_{i})$$

$$- c_{1}^{\ell} (q_{i} - q_{t}) - c_{2}^{\ell} (p_{i} - p_{t})$$

$$(4)$$

In this control protocol, the pair  $(q_t, p_t)$  is the position and velocity of the moving target respectively.  $(c_1^{\alpha}, c_2^{\alpha}), (c_1^{\beta}, c_2^{\beta}),$  and  $(c_1^{\ell}, c_2^{\ell})$  are positive constants. The  $\sigma$ -norm,  $\|.\|_{\sigma}$  of a vector is a map  $R^m \Longrightarrow R_+$  defined as  $\|z\|_{\sigma} = \frac{1}{\varepsilon} [\sqrt{1 + \varepsilon} \|z\|^2 - 1]$ .  $\phi_{\alpha}(z)$  and  $\phi_{\beta}(z)$  are the action functions to control the attractive or repulsive forces between robot i and its neighbor j, and the repulsive force between robot i and its obstacle k, respectively.  $n_{ij}$  and  $f_{kg}$  are the vectors along the line to connect the pair  $(q_i, q_j)$ , and the pair  $(f_{kg}, q_i)$ , respectively.  $a_{ij}(q)$  and  $b_{i,k}(q)$  are adjacency matrices. More details of the these terms, see [10].

The dynamic target is deChed as follows:

$$\begin{cases}
d\vec{p}_t = p_t \\
d\vec{p}_t = f_t(q_t, p_t)
\end{cases}$$
(5)

In the control protocol (4), the Œrst two terms are used to control the formation (collision avoidance and velocity matching among robots). The third and fourth terms are used to allow robots avoiding obstacles. The last terms is used for target tracking. If the last term is absent the control will lead to the fragmentation of the robot network [10].

#### B. Problem Formulation

The problem here is to Chad out the optimal solution of coef Ceients of the interaction forces  $(c_1^{\alpha}, c_2^{\alpha}), (c_1^{\beta}, c_2^{\beta}), (c_1^{t}, c_2^{t})$ which deliver desired swarm robots-like behavior to minimize the normalized cost function (7) while maintaining the  $\alpha$ lattice formation. Namely, the pair  $(c_1^{\alpha}, c_2^{\alpha})$  is used to adjust the attractive/repulsive forces among agent i and its actual neighbors ( $\alpha$ -agent), and the pair  $(c_1^{\beta}, c_2^{\beta})$  is used to adjust the repulsive forces among agent i and its virtual neighbors (βagent) that is generated from agent i when it see the obstacles, and the pair  $(c_1^t, c_2^t)$  is used to adjust the attractive forces between agent i and its target. The bigger  $(c_1^t, c_2^t)$  the faster convergence to the target. However if  $(c_1^t, c_2^t)$  is too big the center of mass (CoM) as defined in Equation (6)

$$\begin{cases} \overline{q} = \frac{1}{n} \sum_{i=1}^{n} q_i \\ \overline{p} = \frac{1}{n} \sum_{i=1}^{n} p_i \end{cases}$$
 (6)

oscillates around the target, and the formation of network is not guaranteed. In addition, in order to guarantee that no agent hit obstacle the pair  $(c_1^{\beta}, c_2^{\beta})$  is selected to be bigger than the other two pairs,  $(c_1^{\alpha}, c_2^{\alpha})$  and  $(c_1^{t}, c_2^{t})$ . Finally we have the relationship among these pairs as:  $(c_{1,2}^{\alpha} < c_{1,2}^t < c_{1,2}^{\beta})$ .

The α-lattice formation can be checked by which is the convergent formation time and is computed based on the condition  $Var(\|q_i-q_j\|)=$  $\frac{1}{|E|}\sum (\|q_i - q_j\| - \frac{1}{n}\sum_{(i,j)\in E}\|q_j - q_i\|)^2 \le \Theta \text{ with } i,j = 1,2,...,$ n, here  $\Theta$  is the given threshold, and  $i \neq j$ , and they are on the same edge  $\in E$ .

$$F = \frac{\sum_{i=1}^{n} \int_{0}^{T} \|q_{i}(t) - q_{t}(t)\| dt}{T \sum_{i=1}^{n} \|q_{i}(t=0) - q_{t}(t=0)\|}$$
(7)

here T is the total simulation time.

The cost function (7) represents the following terms:

-The time it takes all robots in the network to catch up the moving target.

-The distance of all robots in the network away from the target.

Clearly see that the function (7) is non-convex and nondifferentiable. Hence to minimize this function the classical gradient-based deterministic optimization methods are unstable because these methods are usually trapped by the local minima. To solve this problem, Genetic Algorithms (GAs), a certain class of non-derivative search techniques, especially advanced GAs [31] such as NSGA II (Non-Dominated Sorting GA) [32], SPEA II (Strength Pareto EA) [33], RDGA (Rank-Densitybased Genetic Algorithm) [34] and a temporally-adaptive iterative scheme of GA [35], etc. can be applied.

The term  $\sum_{i=1}^{n} ||q_i(t=0) - q_t(t=0)||$  in denominator of (7) is the total distance between all robots and the target at initial time. We see that this is the maximum distance because at initial time all robots are furthest from the target. In addition, the term  $\sum_{i=1}^{n} \|q_i(t) - q_t(t)\|$  is the total distance between all robots and the target at time t. This distance will be decreased during tracking process when all robots apply the cocking algorithm (4), and this leads to  $\sum_{i=1}^{n} \int_{0}^{T} ||q_{i}(t) - q_{t}(t)|| dt$  also

decreasing. The question here is how fast the cost function (7) decreases. This depends on how the coef**G**eients  $(c_1^{\alpha}, c_2^{\alpha})$ ,  $(c_1^{\beta}, c_2^{\beta}), (c_1^t, c_2^t)$  are sought. The answer of this question will be found after the function (7) is minimized by advanced GAs.

## III. OPTIMAL DESIGN OF FLOCKING CONTROL VIA GENETICS ALGORITHM

In this section, a genetic algorithm will be developed to deal with the non-convexity of the function (7) in the cocking control design. The similar idea of this approach can be found in [35]. The main idea here is that the cocking parameters form a genetic string and then it is tested via the objective function. A survival one is applied to a population in such string. The entire process is stated as follows.

**Step 1.** A population (M) of different designs are generated randomly with Gaussian distribution in the certain searching space. The genetic strings here are represented for the design parameters (6 cocking parameters as shown above).

**Step 2.** The performance of each design is tested via the objective function. The best genetic string is the one with the smallest objective function. Especially, if some conditions (see pseudo code) are not satisæd this genetic string will be eliminated and replaced by the new one.

Step 3. The designs are ranked from the top to the bottom according their performance which base on the Œness values.

Step 4. The best designs are mated pairwise producing two offsprings. Namely, each best pair exchanges information by taking random convex combinations of design components of the parents s genetic strings.

Step 5. The worst performing genetic strings are eliminated.

Step 6. New replacement strings are added into the remaining population of best performing genetic strings.

The pseudo code of optimal design of cocking control via genetics algorithm is given as below.

**1.** Randomly generate M starting genetic strings.

$$\begin{split} &\Omega^{I} = (\omega_{1}^{I}, \omega_{2}^{I}, \omega_{3}^{I}, \omega_{4}^{I}, \omega_{5}^{I}, \omega_{6}^{I},) = \\ &= (c_{1}^{\alpha}, \ c_{2}^{\alpha}, \ c_{1}^{\beta}, \ c_{2}^{\beta}, \ c_{1}^{I}, \ c_{2}^{\prime})^{I}, \ I = 1, 2 ..., M. \\ &\textbf{2. Compute Geness of each genetic string } I, \ I = 1, 2 ..., M. \end{split}$$

Test each genetic string I, and if some conditions are satis Ged then compute its Geness value via Geness function  $F(\Omega^I)$ .

$$\begin{aligned} & \textbf{for } k = 1 \text{ to } K_d \textbf{ do} \\ & \textbf{for } i = 1 \text{ to } n \textbf{ do} \\ & \text{Update position of robot } i. \\ & q_i(k+1) = q_i(k) + \frac{p_i(k)}{\Delta_t} + \frac{u_i(k+1)}{\Delta_t^2}. \\ & \text{Update velocity of robot } i. \\ & p_i(k+1) = \frac{q_i(k+1) - q_i(k)}{\Delta_t}. \\ & \text{Compute iteration difference.} \\ & diff(i) = \|q_i(k+1) - q_i(k)\|. \\ & \text{Compute error.} \\ & e(k) = \frac{\sum_{i=1}^n diff(i)}{\sum_{i=1}^n \|q_i(k+1)\|}. \\ & \text{Check the convergent distance } T_{cd} \text{ and the convergent formation } T_{cf}. \\ & T_{cd} = \|\frac{1}{n} \sum_{i=1}^n q_i(k) - q_t(k)\|. \\ & T_{cf} = \frac{1}{|E|} \sum (\|q_i - q_j\| - \frac{1}{n} \sum_{(i,j) \in E} \|q_j - q_i\|)^2. \end{aligned}$$

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if e(k) \leq \Theta_1, T_{cd} \leq \Theta_2, T_{cf} \leq \Theta_3, and k < K_d then
               Compute the Eness function.
          F(\Omega^I) = \frac{\sum_{i=1}^n \int_0^T \|q_i(t) - q_t(t)\| dt}{T\sum_{i=1}^n \|q_i(t) - q_t(t)\|}.

else if One of (e(k), T_{cd}, T_{cf}) is not satisfying, and
           k < K_d then
               Jump to next iteration k = k + 1
           else
               Not accepting this genetic string and replacing by
               the new one
           end if
   end for
end for
```

- **3**. Rank the genetic strings,  $\Omega^{I}(I=1,2,...,M)$
- 4. Mate the nearest pairs.

 $\begin{array}{l} \omega^I = c_r^1 \Omega^I + (1-c_r^1) \Omega^{I+1}. \\ \omega^I = c_r^2 \Omega^I + (1-c_r^2) \Omega^{I+1}, \; (c_r^1, c_r^2) \in [0, \; 1] \; \text{are the random} \end{array}$ crossover rates.

- **5**. Kill the botom genetic strings (B < M) and keep the top K parents.
- **6.** New parrents =  $K \cup B_{new}$  then repeat with each  $\Omega^I$  =  $\omega^{I}(I=1,2,...,M).$

In this pseudo code, M is the number of genetic strings,  $K_d$ is the desired iterations, and n is the number of robots.  $q_i(0)$ is randomly distributed in a certain space, and  $p_i(0)$  is set to zero.  $\Theta_1, \Theta_2$  and  $\Theta_2$  are the given thresholds.  $B_{new}$  is the new genetic strings to be introduced into the top K parents.

## IV. EXPERIMENTAL TESTS

In this section we consider the trajectory of the moving target being the sine wave trajectory. The reason for selecting the sine wave trajectory is that the velocity of target in this trajectory keeps changing in whole simulation. Parameters used in this simulation are speciæd as follows:

- Parameters of GAs: the searching space of cocking parameters is setup as  $1 < (c_1^{\alpha}, c_2^{\alpha}) < 100, 100 < (c_1^{\beta}, c_2^{\beta}) < 1500,$  $1 < (c_1^t, c_2^t) < 100$ . The number of genetic strings is M = 15, and the top ten offsprings are selected in each generation. The total generation is set to G = 15. The desired iteration  $K_d = 400$ . The total simulation time is computed as  $T = \Delta_t * K_d$ .
- Parameters of cocking: number of sensors = 115 (randomly distributed in the box [0 100]x[0 100]). Positions of obstacles  $y_k = [260 \ 135; \ 260 \ 195]^T$ ; Radii of obstacles  $R_k =$ [ 20; 20; 4], and other parameters a = b = 5; the interaction range r = 7.8;  $\varepsilon = 0.1$  for the  $\sigma$ -norm; h = 0.2 for the bump function  $(\phi_{\alpha}(z))$ ; h = 0.9 for the bump function  $(\phi_{\beta}(z))$ .
- Parameters of target tracking: The target moves in the sine wave trajectory:  $q_t = [100 + 35t, 135 - 35sin(t)]^T$  with  $0 \le t \le 8$ , and  $p_t = (q_t(t) - q_t(t-1))/\Delta_t$ ,, and  $p_t = (q_t(t) - q_t(t-1))/\Delta_t$

Figure 2 (a) shows the result of Eness function for the case of 45 agents. M = 15 is the total number of genetic strings in the population and K = 10 is the number of parents kept in each generation, or the last four parents B = 5 are killed after each generation. Figure 2 (b) depicts the tracking performances of the various size of agents. These tracking performances represent the errors between the mean of positions of all mobile sensors and the position of target. As shown in this Ggure, all errors go to near zero after 180 iterations.

Figures 2 (c) and 3 represent the results of the moving target tracking in the sine wave trajectory using œocking algorithm (4) with the optimal parameters,  $(c_1^{\alpha}, c_2^{\alpha}), (c_1^{\beta}, c_2^{\beta}), (c_1^{t}, c_2^{t}),$  as shown in the Table 1. In these Gures we see that all mobile sensors (115) track the moving target in the free space (without obstacles) very well with small error, or all mobile sensors can surround the target. However, in the obstacle space, the error between the mean of positions of all sensors and the position of target as shown in Figures 2 (c) is remarkable. This phenomenon can be explained in the Remark 1.

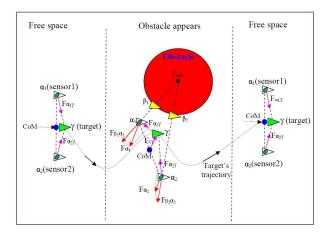


Fig. 1. Demonstration of two sensors tracking the moving target in both free and obstacle spaces.

**Remark 1.** To explain why the tracking performance in presence of obstacles is not good as in the free space, we analyze the forces acting on the  $\alpha$ -agents (sensors) when they pass through the obstacles as shown in the Figure 1. In this General, without losing general we simply consider two sensors tracking the target (y-agent) which moves in arbitrary trajectory.

Firstly, when two sensors track the target in the free space (without obstacle), in the equilibrium state the CoM (Center of Mass) declined as (6) is close to the target (in this case sensor2 is the neighbor of sensor1). The total interaction forces between two sensors are equal to zero, and also because of velocity matching the the sum of different velocities between these sensors is equal to zero. Hence from (4) we have:

$$\overline{u} = \frac{1}{n} \sum_{i=1}^{n} u_i = -(c_1^t)(\overline{q} - q_t) - (c_2^t)(\overline{p} - p_t)$$
 (8)

The Equation (8) means that the CoM  $(\overline{q}, \overline{p})$  converges to the target  $(q_t, p_t)$  (more details please see [26]).

When these sensors move in the obstacle space (the obstacle in the sensing ranges of both sensors) the projection of each sensor on the surface of obstacle is called β-agent (virtual agent). In this scenario, two  $\beta$ -agents,  $\beta_1$  and  $\beta_2$ , of two sensor1 and sensor2 are created, respectively (see Figure 1).

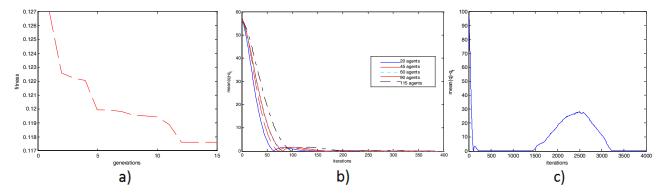


Fig. 2. (a) The values of Offeness function during 15 generations for 45 agents case, (b) Errors between the mean of positions of all mobile sensors and the position of target for only 400 iterations, (c) Error between the mean of positions of all mobile sensors and the position of target for whole tracking process in the case of 115 agents.

 $\label{table I} The \ optimal \ coefficients \ for \ various \ sizes \ of \ flocking \ control.$ 

Number of agents	$c_1^{\alpha}$	$c_2^{\alpha}$	$c_1^t$	$c_2^t$	$c_1^{\beta}$	$c_2^{\beta}$
20	31.99523	23.32457	45.05901	32.92191	919.91231	52.57912
45	33.00721	24.65109	46.08719	34.66901	940.15267	56.33411
60	35.32712	25.66322	46.45919	36.67810	949.91510	64.45910
90	38.79923	26.73234	47.13214	39.74959	1090.92536	70.53211
115	41.48864	26.89120	50.29770	43.87073	1200.88581	71.44092

These  $\beta$ -agents generate the repulsive forces,  $F_{\beta,1}\alpha_1$  and  $F_{\beta_2\alpha_2}$ to push these sensors away from the obstacle. However, the presence of γ-agent (target) is necessary to steer both sensors around the obstacle. The synthesized forces  $\vec{F}_{\alpha_1} = \vec{F}_{\beta_1 \alpha_1} + \vec{F}_{\alpha_1 \gamma}$ and  $\vec{F}_{\alpha_2} = \vec{F}_{\beta_{12}\alpha_2} + \vec{F}_{\alpha_2\gamma}$  of sensor1 and sensor2, respectively. To avoid each sensor hitting the obstacle the weights of repulsive force of the obstacle  $c_1^{\beta}, c_2^{\beta}$  are set bigger than that of attractive force between the target and each sensor  $c_1^t, c_2^t$ , this leads to the force  $F_{\beta_1\alpha_1} > F_{\alpha_1\gamma}$  and  $F_{\beta_2\alpha_2} > F_{\alpha_2\gamma}$ . This causes these sensors being pushed away in a certain distance from the target, or the CoM is no longer close to the target. Otherwise, in general situation (more than two sensors) a sensor i might stay near a distance  $r_0$  (0 <  $r_0$  < r) from the obstacle for a long time due to fpeerpanicf by other sensors j that are on the way of sensor i and keep sensor i back [36]. In all above simulation results, all sensors keep their formation and no collision occurs among them while tracking the moving target, and all sensors avoid obstacles successfully in a narrow space. For more details please see the video (He posted in the below link:

http://www.youtube.com/watch?v = 5dfdo4L07jY

# V. CONCLUSION

This paper studied the optimization problem in the distributed cocking control for a mobile sensor network to track a moving target. The non-convex objective function was constructed, then the optimization method based on GAs was developed. The optimal cocking coef ceients for various size of members in cocking control algorithm were found out. Analysis of the cocking behavior based moving target tracking in both free space and obstacle space is given. The numerical tests were shown to validate our approach.

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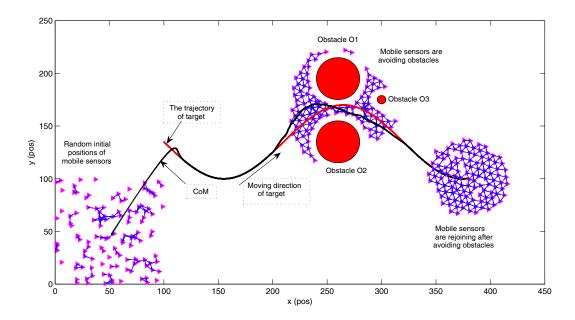


Fig. 3. Snapshots of the beginning positions, avoiding obstacles positions and ending positions of 115 mobile sensors which are tracking the target moving in the sine wave trajectory.

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